

§7-4 Factored Form of a Quadratic Function

* Relate the factors of a quadratic function to the characteristics of its graph.

$$y = a(x-r)(x-s)$$

Example 1 (p383)

Sketch the graph of the quadratic function:

$$f(x) = 2x^2 + 14x + 12$$

State the domain and range.

(no table of values
+ calculator)

$$f(x) = 2x^2 + 14x + 12$$

$$f(x) = 2(x^2 + 7x + 6)$$

factored form $\rightarrow (f(x) = 2(x+6)(x+1))$

Find the x-intercepts (zeros) by setting equal to 0.

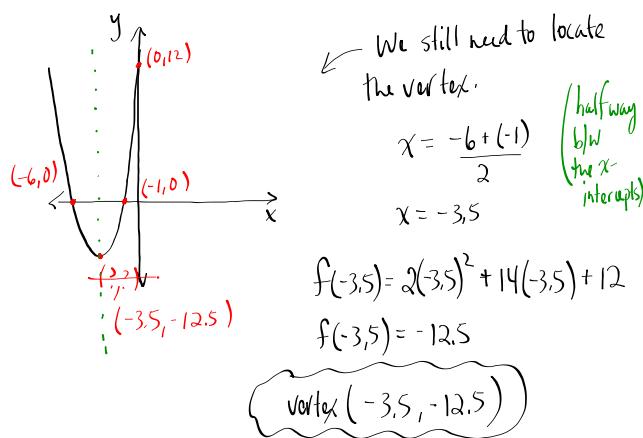
$$0 = 2(x+6)(x+1)$$

Set each factor equal to zero & solve for x:

$$\begin{aligned} x+6=0 &\quad x+1=0 \\ x=-6 &\quad \text{roots} \quad x=-1 \\ (-6, 0) &\quad \text{x-intercepts} \quad (-1, 0) \end{aligned}$$

The y-intercept is c ($ax^2 + bx + c$)

so the y-intercept is 12 or the point (0, 12)



When sketching a graph of a quadratic:

- ① x-intercepts
- ② y-intercept
- ③ vertex/axis of symmetry

domain: $\{x | x \in \mathbb{R}\}$

range: $\{y | y \in \mathbb{R}, y \geq -12.5\}$

Example 2 - Partial factoring

Sketch the graph of the following quadratic function:

$$f(x) = x^2 + 6x + 10 \quad -(x^2 - 6x - 10)$$

State the domain
+ range

$$f(x) = \underbrace{x(x-6)}_{\text{factor this part}} + 10$$

Set equal to zero

Set each factor equal to zero

$$-x(x-6) = 0$$

$$\begin{cases} x=0 \\ x=6 \end{cases}$$

point $(0, 10)$

$$x-6 = 0$$

$$\begin{cases} x=6 \\ x=0 \end{cases}$$

point $(6, 10)$

These points have the same y-value.

The vertex is located half way between.

$$\text{vertex: } x = \frac{0+6}{2}$$

$$x = 3$$

$$(3, 19)$$

$$f(x) = -x^2 + 6x + 10$$

$$f(3) = -(3)^2 + 6(3) + 10$$

$$f(3) = -9 + 18 + 10$$

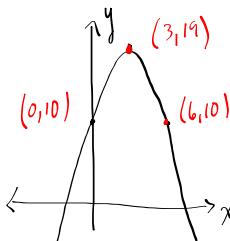
$$f(3) = 19$$

points: $y_{int} (0, 10), (6, 10)$

vertex: $(3, 19)$

y-intercept: $(0, 10)$

graph opens down.



domain: $\{x | x \in \mathbb{R}\}$

range: $\{y | y \in \mathbb{R}, y \leq 19\}$

If the quadratic factors easily:

- Example 1*
- ① set equal to zero to find x-intercepts.
 - ② find vertex (halfway between x-intercepts)
 - ③ find y-intercept

If the quadratic doesn't factor easily, we partial

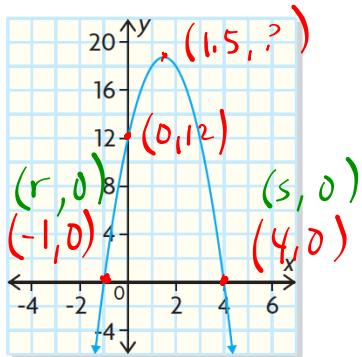
- Example 2*
- ① set first part equal to zero to find two points with same y-value
 - ② find the vertex (halfway between two points)
 - ③ find y-intercept.

Example 3 - Find the equation from the graph.

Determining the equation of a quadratic function, given its

tion that defines this parabola. Write the function in

$$\begin{aligned}x &= \frac{-1+4}{2} \\x &= \frac{3}{2} \\x &= 1.5\end{aligned}$$



factored form
 $y = a(x-r)(x-s)$

r and s are
the x -intercepts

$$\begin{aligned}y &= a(x-(-1))(x-4) \quad \text{sub in values for} \\&\qquad\qquad\qquad \text{the } x\text{-intercepts.} \\y &= a(x+1)(x-4)\end{aligned}$$

In order to find a , we need a point (x,y) to sub in. Do not use the x -intercepts.

use $(0, 12)$

$$12 = a(0+1)(0-4)$$

$$12 = a(1)(-4)$$

$$12 = a(-4)$$

$$a = -3$$

$y = -3(x+1)(x-4)$

To Do:

① C4u (p391)

② p391 | 4-13

Read Summary

p390